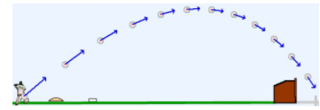
23.1.1 MG road-map: Projectile motion (2D)

A baseball (particle Q) flies over Earth N (a Newtonian reference frame). Aerodynamic forces on the baseball are modeled as $-b\,\vec{\mathbf{v}}$ ($\vec{\mathbf{v}}$ is Q's velocity in N).
$\widehat{\mathbf{n}}_x$ is horizontally-right, $\widehat{\mathbf{n}}_y$ is vertically-upward, and N_o is home-plate (point fixed in N).



MG road-map for projectile motion x and y ($\widehat{\mathbf{n}}_x$, $\widehat{\mathbf{n}}_y$ measures of Q's position vector from N_o)

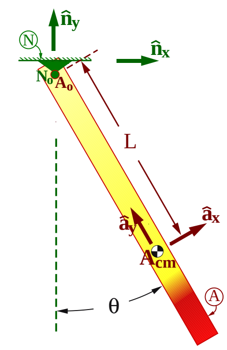
Variable	Translate/ Rotate	Direction (unit vector)	System S	FBD of S	About point	*MG road-map equation*
x				Draw	Not applicable	· ($\overset{(22.1)}{=}$)
y				Draw	Not applicable	· ($\overset{(22.1)}{=}$)

x	Dot(, .GetDynamics( ))	**M**otion**G**enesis command ©
y	Dot(, .GetDynamics( ))	**M**otion**G**enesis command ©

Draw FBD

Solution and simulation link at **www.MotionGenesis.com** ⇒ **Textbooks** ⇒ **Resources**.

23.1.2 MG road-map: Rigid body pendulum (2D)



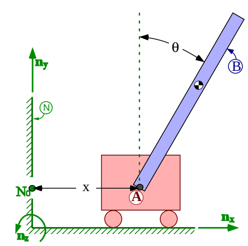
A non-uniform density rigid rod A is attached at point A_o of A by a frictionless revolute/pin joint to Earth N (Newtonian reference frame). The rod swings with a "pendulum angle" θ in a vertical plane that is perpendicular to unit vector $\widehat{\mathbf{a}}_z$.

Variable	Translate/ Rotate	Direction (unit vector)	System S	FBD of S	About point	*MG road-map equation*
θ				Draw		· ($\overset{(22.4)}{=}$)

θ	Dot(, .GetDynamics( ))	**M**otion**G**enesis command ©

Solution and simulation link at **www.MotionGenesis.com** ⇒ **Textbooks** ⇒ **Resources**.

23.1.3 MG road-map: Inverted pendulum on cart (x and θ) (2D)



A rigid rod B is pinned to a massive cart A (modeled as a particle) that translates horizontally in a Newtonian reference frame N. The cart's position vector from a point N_o fixed in N is $x\,\widehat{\mathbf{n}}_x$ ($\widehat{\mathbf{n}}_x$ is horizontally-right). B's swinging motion in N is in a vertical plane perpendicular to $\widehat{\mathbf{n}}_z$ (a unit vector fixed in both B and N).

Variable	Translate/ Rotate	Direction (unit vector)	System S	FBD of S	About point	*MG road-map equation*
x				Draw	Not applicable	· ($\overset{(22.1)}{=}$)
θ				Draw		· ($\overset{(22.4)}{=}$)

x		**M**otion**G**enesis command ©
θ		**M**otion**G**enesis command ©

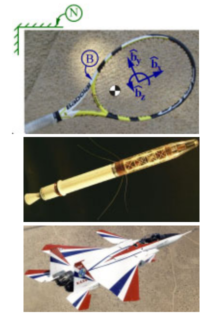
Homework 19.8 and Chapter 30 complete these calculations.

23.1.4 MG road-map: Rotating rigid body (3D)

Shown right is a rotating rigid body B (e.g., tennis racquet, spacecraft, or aircraft) in a Newtonian reference frame N. Right-handed orthogonal unit vectors $\widehat{\mathbf{b}}_x$, $\widehat{\mathbf{b}}_y$, $\widehat{\mathbf{b}}_z$ are fixed in B.

Variable	Translate/ Rotate	Direction (unit vector)	System S	FBD of S	About point	*MG road-map equation*
ω_x				Draw		$\cdot\,(\quad \underset{(22.4)}{=} \quad)$
ω_y				Draw		$\cdot\,(\quad \underset{(22.4)}{=} \quad)$
ω_z				Draw		$\cdot\,(\quad \underset{(22.4)}{=} \quad)$

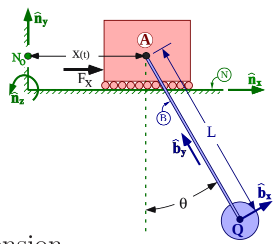
ω_x	**Dot(** , **.GetDynamics(** **))**	**M**otion**G**enesis command ©
ω_y	**Dot(** , **.GetDynamics(** **))**	**M**otion**G**enesis command ©
ω_z	**Dot(** , **.GetDynamics(** **))**	**M**otion**G**enesis command ©



Solution and simulation link at **www.MotionGenesis.com** ⇒ **Textbooks** ⇒ **Resources**.

Note: The "about point" is somewhat arbitrary. When B_{cm} is chosen: $^N\vec{H}^{B/B_{cm}} \underset{(17.2)}{=} \vec{\vec{I}}^{B/B_{cm}} \cdot {}^N\vec{\omega}^B$.

23.1.5 MG road-map: Bridge crane equations of motion (2D)



A payload (particle) Q is welded to a light rigid cable B which swings in a Newtonian frame N. Cable B is pinned to a massive trolley A that can move horizontally along a smooth slot fixed in N with a **specified** (known) displacement $x(t)$. A translational actuator with force measure F_x connects trolly A to point N_o of N.

MG road-map for pendulum angle θ, actuator force F_x, and cable tension

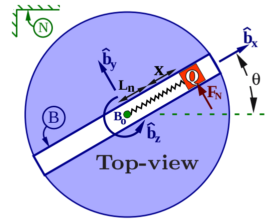
Variable	Translate/ Rotate	Direction (unit vector)	System S	FBD of S	About point	*MG road-map equation*
θ				Draw		
F_x				Draw	Not applicable	
Tension				Draw	Not applicable	

θ	**Dot(** , **System(** **).GetDynamics(** **))**	**M**otion**G**enesis command ©
F_x	**Dot(** , **System(** **).GetDynamics( ))**	**M**otion**G**enesis command ©

Student/Instructor version at **www.MotionGenesis.com** ⇒ **Textbooks** ⇒ **Resources**

Note: Only the θ road-map equation is needed to predict this system's motion. The others are shown for illustrative purposes.

23.1.6 MG road-map: Particle on spinning slot (2D)



A particle Q slides on a straight slot B. The slot is connected with a revolute joint to a Newtonian frame N at point B_o so that B rotates in a horizontal plane perpendicular to $\hat{\mathbf{b}}_z$ ($\hat{\mathbf{b}}_z$ is vertically-upward and fixed in both B and N).

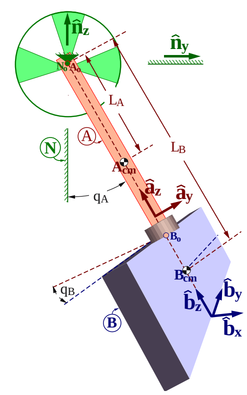
Note: Homework 18.8 completes the MG road-map calculations for x and θ.

MG road-map for x, θ, and F_N ($\hat{\mathbf{b}}_y$ measure of normal force on Q from B)

Variable	Translate/ Rotate	Direction (unit vector)	System S	FBD of S	About point	***MG road-map equation***
x				Draw	Not applicable	$\cdot$ ($=$)
θ				Draw	B_o	$\cdot$ ($=$)
F_N				Draw	Not applicable	$\cdot$ ($=$)
x	**Dot(, .GetDynamics())**					**M**otion**G**enesis command ©
θ	**Dot(, System( ).GetDynamics( ))**					**M**otion**G**enesis command ©
F_N	**Dot(, .GetDynamics())**					**M**otion**G**enesis command ©

Note: The F_N road-map equation is needed to predict motion **if** a friction force depends on $\mu\, F_N$.

23.1.7 MG road-map: Motion of a chaotic double pendulum (3D)



Shown right is a mechanical model of a swinging babyboot (uniform plate B) attached by a shoelace (thin uniform rod A) to a fixed rigid support N. Rod A is attached to N by a revolute joint at point N_o of N. B is attached to A with a second revolute joint at point B_o so B can rotate freely about A's axis.

Note: The revolute joints' axes are ***perpendicular***, not parallel.

- The plate, rod, and support are rigid.
- The revolute joints are ideal (massless, frictionless, no slop/flexibility).
- Earth is a Newtonian reference frame N.
- Forces due to Earth's gravitation are uniform and constant.
- Other distance forces (electromagnetic and gravitational) and air-resistance are negligible.

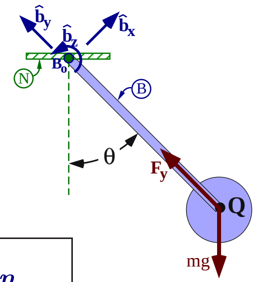
Right-handed sets of unit vectors $\hat{\mathbf{n}}_x$, $\hat{\mathbf{n}}_y$, $\hat{\mathbf{n}}_z$; $\hat{\mathbf{a}}_x$, $\hat{\mathbf{a}}_y$, $\hat{\mathbf{a}}_z$; $\hat{\mathbf{b}}_x$, $\hat{\mathbf{b}}_y$, $\hat{\mathbf{b}}_z$ are fixed in N, A, B, respectively, with $\hat{\mathbf{n}}_x = \hat{\mathbf{a}}_x$ parallel to the revolute axis joining A to N, $\hat{\mathbf{n}}_z$ vertically-upward, $\hat{\mathbf{a}}_z = \hat{\mathbf{b}}_z$ parallel to the rod's long axis (and the revolute axis joining B to A), and $\hat{\mathbf{b}}_z$ perpendicular to plate B. q_A is the angle from $\hat{\mathbf{n}}_z$ to $\hat{\mathbf{a}}_z$ with $+\hat{\mathbf{n}}_x$ sense. q_B is the angle from $\hat{\mathbf{a}}_y$ to $\hat{\mathbf{b}}_y$ with $+\hat{\mathbf{a}}_z$ sense.

Variable	Translate/ Rotate	Direction (unit vector)	System S	FBD of S	About point	***MG road-map equation***
q_A				Draw		$\cdot$ ($=$)
q_B				Draw		$\cdot$ ($=$)
q_A	**Dot(, System( ).GetDynamics( ))**					**M**otion**G**enesis command ©
q_B	**Dot(, .GetDynamics( ))**					**M**otion**G**enesis command ©

Solution and simulation link at **www.MotionGenesis.com** ⇒ **Textbooks** ⇒ **Resources**.

Note: The "about point" for the q_B road-map can be shifted from B_o to B_{cm} since $\hat{\mathbf{b}}_z \cdot \vec{\mathbf{M}}^{B/B_{cm}} \underset{(19.4)}{=} \hat{\mathbf{b}}_z \cdot \vec{\mathbf{M}}^{B/B_o}$.

23.1.8 MG road-map: Particle pendulum (2D) – angle and tension



A particle Q is welded to the distal end of a light rigid rope B. The rope's other end attaches to a point B_o, fixed in a Newtonian reference frame N. The swinging motion of B and Q is in a vertical plane that is perpendicular to unit vector $\widehat{\mathbf{b}}_z$.

MG road-map for pendulum angle θ and tension F_y ($\widehat{\mathbf{b}}_y$ measure of force on Q from B)

Variable	Translate/ Rotate	Direction (unit vector)	System S	FBD of S	About point	***MG road-map equation***
θ				**Draw**		$\cdot$ ($=$ (22.4))
F_y				**Draw**	Not applicable	$\cdot$ ($=$ (22.1))
θ						**M**otion**G**enesis command ©
F_y						**M**otion**G**enesis command ©

Draw FBDs

Solution and simulation link at **www.MotionGenesis.com** ⇒ **Textbooks** ⇒ **Resources**.
Note: Only the θ road-map equation is needed to predict motion. The other is shown for illustrative purposes.

23.1.9 MG road-map: Dynamicist on a turntable (ice-skater)

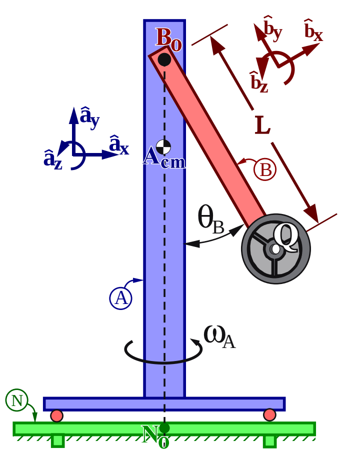
A dynamics instructor stands on a spinning turntable and swings a heavy dumbbell Q inward and outward to change his spin-rate (similar to the ice-skater).
Q is modeled as a particle rigidly attached (welded) to the end of the instructor's hands.

The schematic (below-right) shows a rigid body A (modeling the instructor's legs, torso, and head) that rotates (without friction) relative to Earth (a Newtonian reference frame N) about a vertical axis that is fixed in both A and N and which passes through both point N_o of N and point A_{cm} (A's center of mass).

A massless rigid arm B (modeling the instructor's arms and hands) attaches to A by a revolute motor (shoulder/muscles) whose revolute axis is horizontal and located at point B_o of B (B_o lies on the vertical axis connecting N_o and A_{cm}).

The motor (muscles) **specifies** B's angle θ_B relative to A to change in a known (prescribed) manner from 0 to π rad in 4 seconds ($\theta_B = \pi \frac{t}{4}$).

Right-handed orthogonal unit vectors $\widehat{\mathbf{a}}_x$, $\widehat{\mathbf{a}}_y$, $\widehat{\mathbf{a}}_z$ and $\widehat{\mathbf{b}}_x$, $\widehat{\mathbf{b}}_y$, $\widehat{\mathbf{b}}_z$ are fixed in A and B, respectively, with $\widehat{\mathbf{a}}_y$ vertically-upward, $\widehat{\mathbf{b}}_z = \widehat{\mathbf{a}}_z$ parallel to the revolute motor's axis, and $\widehat{\mathbf{b}}_y$ directed from Q to B_o.



Quantity	Symbol	Type	Value
Earth's gravitational constant	g	Constant	$9.8\ \frac{m}{s^2}$
Distance between Q and B_o	L	Constant	0.7 m
Mass of Q	m	Constant	12 kg
A's moment of inertia about line $\overline{A_{cm}\,B_o}$	I_{yy}	Constant	$0.6\ \text{kg m}^2$
Angle from $\widehat{\mathbf{a}}_y$ to $\widehat{\mathbf{b}}_y$ with $^+\widehat{\mathbf{a}}_z$ sense	θ_B	**Specified**	$\mathbf{0.25\,\pi\,t}$ rad
$\widehat{\mathbf{a}}_y$ measure of A's angular velocity in N	ω_A	Variable	

Complete the ***MG road-map*** for the turntable's "spin-rate" ω_A (Note: The "about point" is not unique)

Variable	Translate/ Rotate	Direction (unit vector)	System S	FBD of S	About point	***MG road-map equation***
ω_A				**Draw**		
ω_A	**Dot(**	**, System(**	**).GetDynamics(**	**))**		**M**otion**G**enesis command ©

Student/Instructor version at **www.MotionGenesis.com** ⇒ **Textbooks** ⇒ **Resources**

23.1.10 MG road-map: Instructor on turntable with spinning wheel (3D)

The pictures to the right shows dynamicist Dr. G standing on a spinning turntable and holding a spinning bicycle wheel.

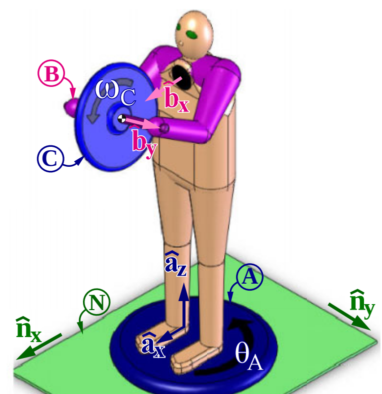
The mechanical model (below right) has a rigid body A (modeling the turntable, legs, torso, and head) that can freely rotate relative to Earth (Newtonian reference frame N) about a vertical axis that is fixed in both A and N and which passes through the center of the turntable (point N_o) and A_{cm} (A's center of mass).

A light (massless) rigid frame B (modeling the shoulders, arms, hands, and a portion of the bicycle wheel's axle) is attached to A by a revolute motor at point B_o of B (B_o lies on the vertical axis passing through A_{cm}). The motor's revolute axis passes through points B_o and C_{cm}, is horizontal, and is parallel to $\widehat{\mathbf{b}}_x = \widehat{\mathbf{a}}_x$.

A rigid bicycle wheel C is attached to B by a frictionless revolute joint whose axis passes through C_{cm} (C's center of mass) and is parallel to $\widehat{\mathbf{b}}_y$.

Right-handed orthogonal unit vectors $\widehat{\mathbf{a}}_x$, $\widehat{\mathbf{a}}_y$, $\widehat{\mathbf{a}}_z$ and $\widehat{\mathbf{n}}_x$, $\widehat{\mathbf{n}}_y$, $\widehat{\mathbf{n}}_z$ are fixed in A and N, respectively. Initially $\widehat{\mathbf{a}}_i = \widehat{\mathbf{n}}_i$ $(i = x, y, z)$, and then rigid body A is subjected to a right-handed rotation characterized by $\theta_A \, \widehat{\mathbf{a}}_z$ where $\widehat{\mathbf{a}}_z = \widehat{\mathbf{n}}_z$ is directed vertically-upward and $\widehat{\mathbf{a}}_x$ points from Dr. G's back to front (parallel to the axis of the revolute motor connecting A and B).

Unit vectors $\widehat{\mathbf{b}}_x$, $\widehat{\mathbf{b}}_y$, $\widehat{\mathbf{b}}_z$ are fixed in B. Initially $\widehat{\mathbf{b}}_i = \widehat{\mathbf{a}}_i$ $(i = x, y, z)$, then B is subjected to a $\theta_B \, (\widehat{\mathbf{a}}_x = \widehat{\mathbf{b}}_x)$ right-handed rotation in A where $\widehat{\mathbf{b}}_y$ is directed along the wheel's axle from Dr. G's right-to-left hand. Dr. G changes θ_B in a **specified** sinusoid manner with amplitude 30° and period 4 seconds.



Courtesy Doug Schwandt
Purchase turntable/bicycle wheel at Arbor-scientific

Quantity	Symbol and type		Value
Mass of C	m^C	Constant	2 kg
Distance between B_o and C_{cm}	L_x	Constant	0.5 m
A's moment of inertia about B_o for $\widehat{\mathbf{a}}_z$	I^A_{zz}	Constant	0.64 kg m²
C's moment of inertia about C_{cm} for $\widehat{\mathbf{b}}_x$	I^C	Constant	0.12 kg m²
C's moment of inertia about C_{cm} for $\widehat{\mathbf{b}}_y$	J^C	Constant	0.24 kg m²
Angle from $\widehat{\mathbf{n}}_x$ to $\widehat{\mathbf{a}}_x$ with $^+\widehat{\mathbf{n}}_z$ sense	θ_A	Variable	
Angle from $\widehat{\mathbf{a}}_y$ to $\widehat{\mathbf{b}}_y$ with $^+\widehat{\mathbf{a}}_x$ sense	θ_B	**Specified**	$\frac{\pi}{6} \sin(\frac{\pi}{2} t)$
$\widehat{\mathbf{b}}_y$ measure of C's angular velocity in B	ω_C	Variable	

Complete the ***MG road-map*** for θ_A and ω_C (the "about points" are not unique).

Variable	Translate/ Rotate	Direction (unit vector)	System S	FBD of S	About point	MG road-map equation
θ_A				**Draw**		
ω_C				**Draw**		

θ_A	**Dot(** ___ **, System(** ___ **).GetDynamics(** ___ **))**	**M**otion**G**enesis command ©
ω_C	**Dot(** ___ **,** ___ **.GetDynamics(** ___ **))**	**M**otion**G**enesis command ©

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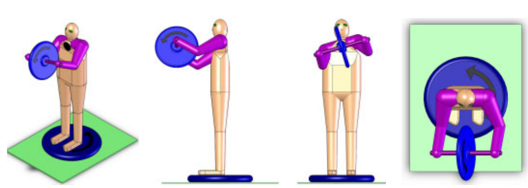
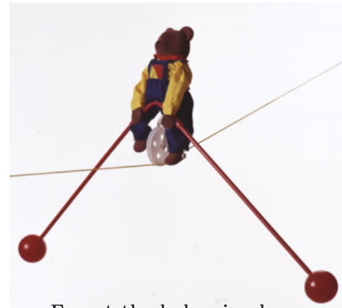


23.1.11 MG road-map: Bear riding a unicycle on a high-wire (3D)



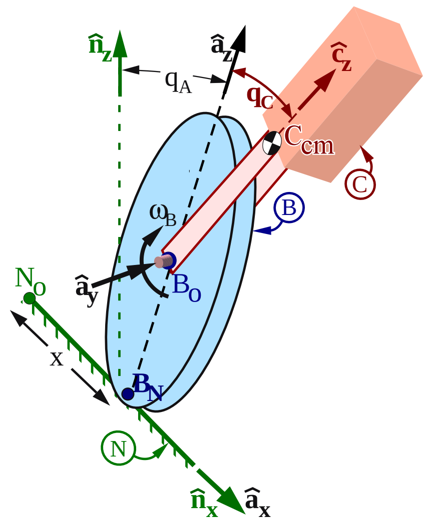
Ernest the balancing bear
Purchase at Schylling toy

The figures to the right show a (massless) pulley-wheel B that **rolls** along a taut (rigid) cable N (fixed on Earth, a Newtonian frame). Rigid body C (seat, rider, and balancing poles) attach to B with an ideal revolute motor at B_o (B's centroid). The motor axis is aligned with B's symmetry axis.

Right-handed orthogonal unit vectors $\hat{\mathbf{n}}_x$, $\hat{\mathbf{n}}_y$, $\hat{\mathbf{n}}_z$ are fixed in N with $\hat{\mathbf{n}}_z$ vertically-upward and $\hat{\mathbf{n}}_x$ directed horizontally along the cable from a point N_o (fixed in N) to B_N (B's rolling point of contact with N).

Right-handed orthogonal unit vectors $\hat{\mathbf{a}}_x$, $\hat{\mathbf{a}}_y$, $\hat{\mathbf{a}}_z$ are directed with $\hat{\mathbf{a}}_x = \hat{\mathbf{n}}_x$, $\hat{\mathbf{a}}_y$ parallel to the motor axis, and $\hat{\mathbf{a}}_z$ from B_N to B_o.

Right-handed unit vectors $\hat{\mathbf{c}}_x$, $\hat{\mathbf{c}}_y$, $\hat{\mathbf{c}}_z$ are parallel to C's principal inertia axes about C_{cm} (C's center of mass), with $\hat{\mathbf{c}}_y = \hat{\mathbf{a}}_y$ and $\hat{\mathbf{c}}_z$ from B_o to C_{cm} (with balancing poles, C_{cm} is below B_o and L_C is negative).



Quantity	Symbol	Type	Value
Earth's gravitational constant	g	Constant	9.8 m/s^2
Radius of B	r_B	Constant	30 cm
$\hat{\mathbf{c}}_z$ measure of C_{cm}'s position vector from B_o	L_C	Constant	–35 cm
Mass of C	m^C	Constant	2 kg
C's moment of inertia about C_{cm} for $\hat{\mathbf{c}}_x$	I	Constant	3.4 kg m^2
C's moment of inertia about C_{cm} for $\hat{\mathbf{c}}_y$	J	Constant	3.2 kg m^2
C's moment of inertia about C_{cm} for $\hat{\mathbf{c}}_z$	K	Constant	2.8 kg m^2
$\hat{\mathbf{a}}_y$ measure of motor torque on B from C	T_y	**Specified**	below
Angle from $\hat{\mathbf{n}}_z$ to $\hat{\mathbf{a}}_z$ with $-\hat{\mathbf{n}}_x$ sense	q_A	Variable	
$\hat{\mathbf{a}}_y$ measure of ${}^A\vec{\boldsymbol{\omega}}^B$ (${}^A\vec{\boldsymbol{\omega}}^B = \omega_B\,\hat{\mathbf{a}}_y$)	ω_B	Variable	
Angle from $\hat{\mathbf{a}}_z$ to $\hat{\mathbf{c}}_z$ with $+\hat{\mathbf{a}}_y$ sense	q_C	Variable	
$\hat{\mathbf{n}}_x$ measure of $\vec{\mathbf{r}}^{\,B_N/N_o}$	x	Variable	

Form a complete set of ***MG road-maps*** for this systems's equations of motion (solution is not unique).
If necessary, add more ***MG road-maps*** so there are the same number of equations as unknowns.

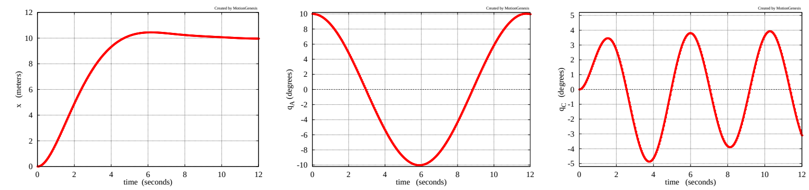
Variable	Translate/ Rotate	Direction (unit vector)	System S	FBD of S	About point	***MG road-map equation***	Additional Unknowns
q_A				**Draw**			
ω_B				**Draw**			
q_C				**Draw**			
x				**Draw**			

* Additional scalar constraint equation(s):
MG road-map for ω_B is not unique. .

q_A	Dot(, System( ).GetDynamics( ))	**M**otion**G**enesis command ©
ω_B	Dot(, System( ).GetDynamics( ))	**M**otion**G**enesis command ©
q_C	Dot(, C.GetDynamics( ))	**M**otion**G**enesis command ©
x	Dot(, System( ).GetDynamics())	**M**otion**G**enesis command ©
	`SolveDt( x' - r*wB = 0,   x' )`	**M**otion**G**enesis command ©

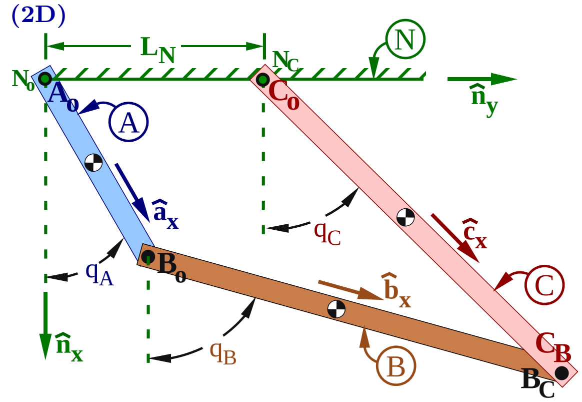
To move the unicycle to $x_{\text{Desired}} = 10$ m, use a "PD control law" with $T_y = -0.3\,(x - x_{\text{Desired}}) - 0.6\,\dot{x}$.

Optional simulation:
Plot x, q_A, q_C for $0 \le t \le 12$ sec.
Use initial values:
$x = 0$ m $q_A = 10°$ $q_C = 0°$
$\dot{x} = 0$ $\dot{q}_A = 0$ $\dot{q}_C = 0$



Solution at **www.MotionGenesis.com** ⇒ **Get Started** ⇒ **Bear on rolling unicycle**.

23.1.12 MG road-map: Four-bar linkage statics (2D)



The figure to the right shows a planar four-bar linkage consisting of frictionless-pin-connected uniform rigid links A, B, and C and ground N.

- Link A connects to N and B at points A_o and A_B
- Link B connects to A and C at points B_o and B_C
- Link C connects to N and B at points C_o and C_B
- Point N_o of N is coincident with A_o
- Point N_C of N is coincident with C_o

Right-handed orthogonal unit vectors $\hat{a}_i$, $\hat{b}_i$, $\hat{c}_i$, $\hat{n}_i$ $(i = x, y, z)$ are fixed in A, B, C, N, with:

- $\hat{a}_x$ directed from A_o to A_B
- $\hat{b}_x$ directed from B_o to B_C
- $\hat{c}_x$ directed from C_o to C_B
- $\hat{n}_x$ vertically-downward
- $\hat{n}_y$ directed from N_o to N_C
- $\hat{a}_z = \hat{b}_z = \hat{c}_z = \hat{n}_z$ parallel to pin axes

As in Hw 10.8, create the following "***loop equation***" and dot-product with $\hat{n}_x$ and $\hat{n}_y$.

$$L_A\,\hat{a}_x + L_B\,\hat{b}_x - L_C\,\hat{c}_x - L_N\,\hat{n}_y = \vec{0}$$

Quantity	Symbol	Value
Length of link A	L_A	1 m
Length of link B	L_B	2 m
Length of link C	L_C	2 m
Distance between N_o and N_C	L_N	1 m
Mass of A	m^A	10 kg
Mass of B	m^B	20 kg
Mass of C	m^C	20 kg
Earth's gravitational acceleration	g	9.81 $\frac{m}{s^2}$
$\hat{n}_y$ measure of force applied to C_B	H	200 N
Angle from $\hat{n}_x$ to $\hat{a}_x$ with $^+\hat{n}_z$ sense	q_A	Variable
Angle from $\hat{n}_x$ to $\hat{b}_x$ with $^+\hat{n}_z$ sense	q_B	Variable
Angle from $\hat{n}_x$ to $\hat{c}_x$ with $^+\hat{n}_z$ sense	q_C	Variable

Complete the following ***MG road-map*** to determine this systems's ***static configuration***.

Variable	Translate/ Rotate	Direction (unit vector)	System S	FBD of S	About point	***MG road-map equation***	Additional Unknowns
				Draw			F^C_x, F^C_y
				Draw			F^C_x, F^C_y
				Draw			F^C_x, F^C_y

* Additional scalar constraint equation: $-L_A\sin(q_A)\,\dot{q}_A - L_B\sin(q_B)\,\dot{q}_B + L_C\sin(q_C)\,\dot{q}_C = 0$

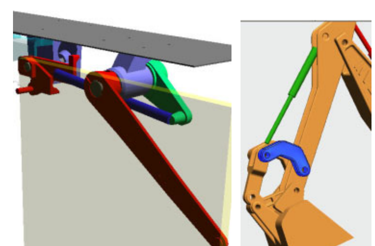
* Additional scalar constraint equation: $L_A\cos(q_A)\,\dot{q}_A + L_B\cos(q_B)\,\dot{q}_B - L_C\cos(q_C)\,\dot{q}_C = 0$

q_A	**Dot(** ___ ,	**System(** ___ **).GetStatics(** ___ **))**	**M**otion**G**enesis command ©
q_B	**Dot(** ___ ,	___ **.GetStatics(** ___ **))**	**M**otion**G**enesis command ©
q_C	**Dot(** ___ ,	**C.GetStatics(** ___ **))**	**M**otion**G**enesis command ©

Determine the ***static equilibrium*** values of q_A, q_B, q_C.
Use your intuition (**guess**), circle the ***stable*** solution.

Solution 1	$q_A \approx 20.0°$	$q_B \approx 71.7°$	$q_C = 38.3°$
Solution 2	$q_A \approx 249.3°$	$q_B \approx 140.2°$	$q_C = 199.1°$
Solution 3	$q_A \approx 30.7°$	$q_B \approx 226.1°$	$q_C = 254.7°$

Solution at **www.MotionGenesis.com** ⇒ **Get Started** ⇒ **Four-bar linkage**



SimWise 4-bar linkages.
Courtesy Design Simulation Technology